

# Predictive Modeling of InGaP/GaAs HBT Noise Parameters from DC and S-Parameter Data for Wireless Power Amplifier Design

James Chingwei Li<sup>1</sup>, Peter J. Zampardi<sup>2</sup>, and Van Pho<sup>3</sup>

<sup>1</sup> UCSD, ECE Dept., 9500 Gilman Dr., MS 0407, La Jolla, CA 92093; (858) 414-0159; [jamescli@alum.mit.edu](mailto:jamescli@alum.mit.edu)

<sup>2</sup> Skyworks Solutions Inc., 2427 W. Hillcrest Dr., MS 889-A02, Newbury Park, CA 91320; (805) 480-4728; [peter.zampardi@skyworksinc.com](mailto:peter.zampardi@skyworksinc.com)

<sup>3</sup> Skyworks Solutions Inc., 20 Sylvan Rd., Woburn, MA 01801; (781) 376-3167; [van.pho@skyworksinc.com](mailto:van.pho@skyworksinc.com)

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## Abstract

Noise characterization of bipolar transistors is typically a lengthy and costly process. As a result, routine monitoring of microwave noise does not generally occur for HBT technologies or products. In contrast, vast quantities of parametric DC data and S-parameter data are measured during the regular course of technology development and production. In work by Voinescu et al [1], DC and S-parameter data are used to predict Silicon BJT and Silicon-Germanium HBT noise parameters. The goal of this work is to apply and adapt, if necessary, the method of [1] to InGaP/GaAs HBTs.

## I. INTRODUCTION

During the technology development and into the product development cycle, it is necessary to periodically examine the noise figure of certain devices and pre-production circuits. This is necessary to ensure that the technology will enable future products to meet design specifications. However, both the equipment and resources required to obtain precise noise parameters throughout the development cycle can be prohibitively expensive. Therefore, it is desirable to develop a method by which noise parameters can be obtained without the use of traditional equipment and leverage already existing measurements.

The composition of a basic noise figure system includes a vector network analyzer, several tuners, noise sources, and a noise figure meter. This suite of equipment easily costs in excess of US\$200,000, and requires a single work shift to produce a complete set of noise parameters for a given device. In contrast, vast quantities of parametric DC data and 50Ω, two-port S-parameter data are obtained by automated test equipment during the regular course of technology and product development. In a method presented by Voinescu et al [1], DC and S-parameter data are used to predict a device's noise parameters. However, the method was applied only to Silicon BJTs and Silicon-Germanium HBTs. The goal of this work is to apply and adapt, if necessary, the method of [1] to InGaP/GaAs HBTs. This would allow technologists and circuit designers to obtain noise parameters from more readily available and less costly measurements.

## II. NOISE MODEL

Although the focus of this paper is noise modeling and characterization, a detailed discussion of noise theory and amplifier noise is not presented here. The reader is referred to Gonzales [2] for additional background material. A review of the noise model and noise parameter formulation presented in [1] follows here.

Fig. 1 shows the  $\pi$ -model small signal equivalent circuit of a bipolar transistor. In addition, the uncorrelated noise sources from terminal resistances,  $r_B$  and  $r_C$ , and the uncorrelated noise currents,  $i_B^2$  and  $i_C^2$ , from junction shot-noise are illustrated. Reduction of these uncorrelated noise sources to their correlated input-referred noise source equivalents,  $v_n^2$  and  $i_n^2$ , is shown in Fig. 2. Visualization of an ideal, noise-free bipolar transistor with two distinct correlated noise sources allows a compact formulation of noise parameters:  $R_n$ , source noise resistance;  $Y_{SOP}$ , the optimum source admittance; and  $F_{MIN}$ , the minimum noise figure in terms of basic device parameters,  $r_B$ ,  $r_E$ ,  $I_B$ ,  $I_C$ , and corresponding Y-parameters. Equations (1)-(5) summarize this formulation. Now that the noise parameters are expressed in terms of measurable quantities,  $I_B$ ,  $I_C$ , [Y], and extracted parameters,  $r_B$ ,  $r_E$ , two port S-parameter measurements are all that are required to complete this analysis method.

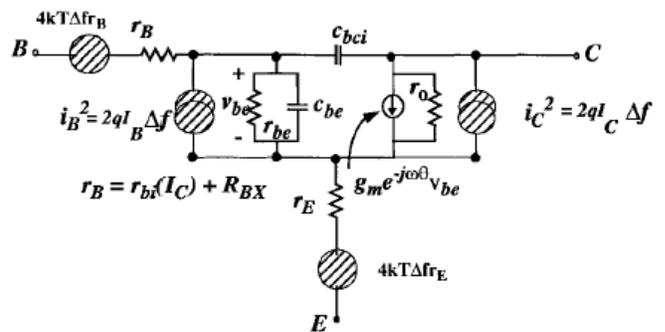


Fig. 1. Small signal and noise equivalent circuit used in the bipolar transistor noise parameter derivation. It features the uncorrelated shot-noise currents  $i_B^2$  and  $i_C^2$ . Reproduced from [1].

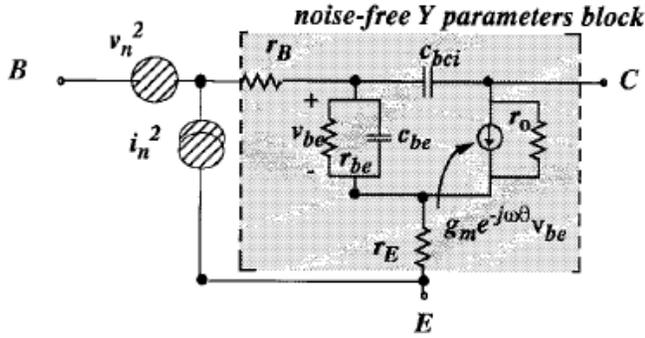


Fig. 2. The equivalent input-referred noise model with correlated noise sources,  $i_n^2$  and  $v_n^2$ , and noise-free  $[Y]$  block. Reproduced from [1].

$$R_n = \frac{I_C}{2V_T |Y_{21}|^2} + (r_E + r_B) \quad (1)$$

$$V_T = \frac{kT}{q} \quad (2)$$

$$\alpha = 2V_T |Y_{21}|^2 (r_E + r_B) \quad (3)$$

$$Y_{SOP} = \sqrt{\frac{I_B |Y_{21}|^2 + I_C |Y_{11}|^2}{\alpha + I_C}} - \left( \frac{I_C \text{Im}\{Y_{11}\}}{\alpha + I_C} \right) - j \frac{I_C \text{Im}\{Y_{11}\}}{\alpha + I_C} \quad (4)$$

$$F_{MIN} = 1 + \frac{I_C}{V_T |Y_{21}|^2} \times \left( \text{Re}\{Y_{11}\} + \sqrt{\left[ 1 + \frac{\alpha}{I_C} \right] \left[ |Y_{11}|^2 + \frac{I_B |Y_{21}|^2}{I_C} \right] - (\text{Im}\{Y_{11}\})^2} \right) \quad (5)$$

### III. EXPERIMENTAL RESULTS

In order to verify the method presented in [1], several devices were manufactured at Skyworks Solutions Inc. Gallium-Arsenide fabrication line in Newbury Park, CA. The process technology features a single hetero-junction HBT, utilizing an InGaP emitter, optimized for wireless communication power amplifiers. For this work, the technology is treated as a black box as the method requires little intimate knowledge of the technology itself. However, discussions in section IV will highlight the need for a greater understanding of the technology in order to refine the noise parameter extraction method.

Noise parameter measurements were performed using an NP5 on-wafer measurement system from ATN Technologies Inc. Since cellular and other commercial wireless communication bands are of interest, only a limited set of measurements between 2 and 6 GHz are presented. Furthermore, measurements focused on a single power amplifier cell configuration with an emitter area of  $56\mu\text{m}^2$  and a larger array of this cell with a total emitter area of  $896\mu\text{m}^2$ . Figs. 3 and 4 present the measured  $F_{MIN}$  and  $G_A$  of the smaller  $56\mu\text{m}^2$  device. Discussion of the larger  $896\mu\text{m}^2$  array will be treated in section V.

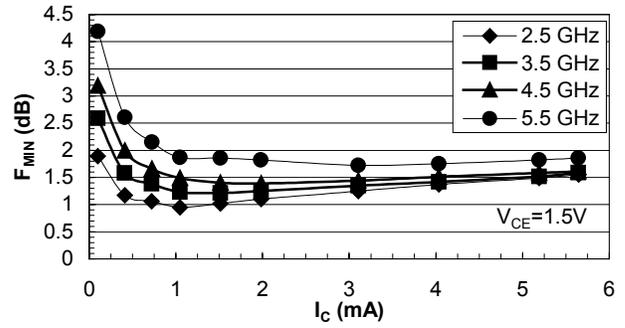


Fig. 3. Measured minimum noise figure as a function of collector current for a  $56\mu\text{m}^2$  InGaP/GaAs SHBT.  $V_{CE}$  is fixed at 1.5V.

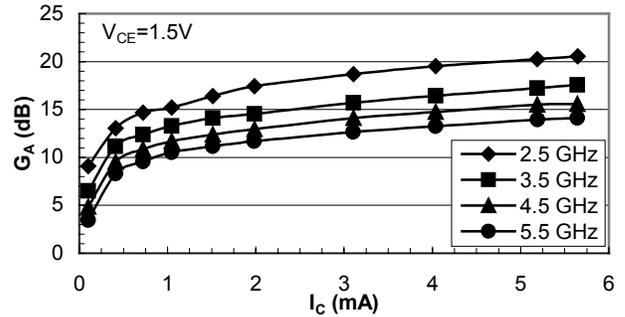


Fig. 4. Measured associated gain,  $G_A$ , as a function of collector current for a  $56\mu\text{m}^2$  InGaP/GaAs SHBT.  $V_{CE}$  is fixed at 1.5.

It is imperative that this work be viewed as a feasibility assessment of a specific noise parameter extraction method to the InGaP/GaAs HBT technology under study. Further measurements and analysis would be required to assess the validity of this method to all GaAs HBT devices and a more general application space.

### IV. NOISE PARAMETER EXTRACTION

In this section, the determination of device parameters necessary for accurate noise parameter prediction will be discussed. The parameter extraction methods described here follow the general practices used by device modelers [1],[3],[4]. Once the appropriate two port  $S$ -parameters are measured for an HBT, the success of the noise parameter extraction process depends heavily on the determination of the emitter resistance,  $r_E$ , and base resistance,  $r_B$ .

First, a value for  $r_B$  is extracted from the real part of  $(Z_{11} - Z_{12})$ . Only frequency values below 1GHz are considered and then averaged to yield an  $I_C$  dependent base resistance,  $r_B(I_C)$ . Fig. 5 shows the extracted  $r_B(I_C)$  as a function of  $I_C$ . Further examination of  $r_B(I_C)$  shows that the  $I_C$  dependency is weak at moderate  $I_C$ , but pronounced at low  $I_C$ . Caution should be exercised when examining the effective  $r_B$  at low  $I_C$  as GaAs HBTs are prone to high base leakage currents and poor base current ideality factors. In addition, this  $r_B(I_C)$

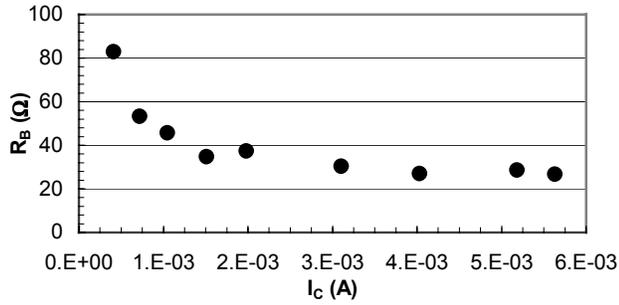


Fig. 5. Base resistance from measured  $S$ -parameters versus collector current

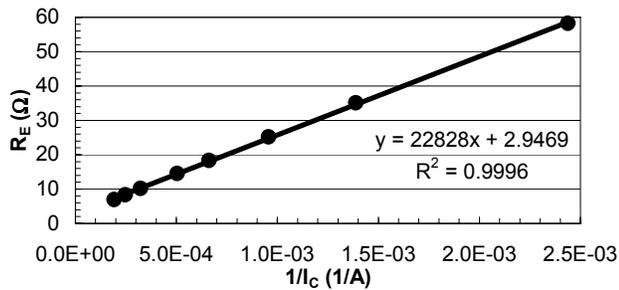


Fig. 6. Emitter resistance from measured  $S$ -parameters versus inverse collector current.

represents the real part of the base impedance, rather than the actual base resistance since, for III-V transistors, the components of the total base resistance are more evenly distributed between intrinsic and extrinsic portions of the device. Even at moderate  $I_C$ , we expect the portion of the  $r_B$  under and surrounding the emitter to show some variation with  $I_C$ , but the majority of the  $r_B$ , composed of the base link region, should be invariant with  $I_C$ . Due to the small range of  $I_C$  considered here, a fixed value of  $25\Omega$  is adopted for the purposes of noise parameter extraction.

The  $r_E$  is determined from the averaged low frequency (<1GHz) values of the real part of  $Z_{12}$  at low  $V_{CE}$  and  $I_C$ . In Fig. 6, the various bias dependent  $\text{Re}\{Z_{12}\}$  values are plotted versus inverse  $I_C$ . The true  $r_E$  can be determined from the y-intercept, and linear regression yields a value of  $2.947\Omega$  for the  $r_E$ . The determination of this parameter is complicated by the pronounced self-heating behavior of GaAs HBTs. It is imperative that  $r_E$  be extracted under minimal bias conditions so that the isothermal condition is maintained. The use of Gummel curves and the  $1/g_m$  versus  $1/I_C$  method is not recommended as the high current region, the region of interest for this method, is highly influenced by device self-heating [5]. The use of RF measurements to determine the small signal equivalent  $r_E$  has produced the best noise parameter extraction results.

Examining equations (1) and (3), we see that  $R_n$  and  $\alpha$  are dependent on the sums of  $r_B$  and  $r_E$ . In the case of the  $56\mu\text{m}^2$  device, the extracted  $r_B$  value is significantly greater than the  $r_E$  value. We would expect  $r_E$  to have little effect on the extracted noise parameters, but an accurate value of  $r_B$  is

crucial. Fig. 7 shows the extracted  $R_n$  versus frequency for various  $I_C$ . Notice that the correlation between extracted and measured noise parameters is reasonable, but the curvature of the experimental data is not parallel to the extracted data. It is expected that  $r_B$ ,  $r_E$ ,  $I_C$ , and  $V_T$  remain constant over frequency, but  $Y_{21}$  could vary considerably.

Further examination of the remaining noise parameters yields additional evidence that the  $Y$ -parameters are the cause of the deviation.  $F_{MIN}$  is plotted on Fig. 8, and the magnitude and phase of  $F_{SOP}$  are plotted on Figs. 9 and 10, respectively.  $F_{MIN}$  is a reasonable fit with no more than 0.2dB deviation, but the extracted curves also have the incorrect curvature. Only  $Y_{11}$  and  $Y_{21}$  are frequency variant quantities located in equation (5). Further deviation is more apparent on the plots of  $F_{SOP}$ . Looking at equations (4) and (5), it is unlikely that  $r_B$ ,  $r_E$ ,  $I_B$ ,  $I_C$ , and  $V_T$  are the cause of the curvature mismatch. However, a systemic error in the  $Y$ -parameter matrix is likely to be cause of the error.

For low power densities, the  $56\mu\text{m}^2$  device has a thermal resistance independent of temperature, and the anticipated rise in junction temperature should be negligible. Under these conditions, we have assumed that the  $56\mu\text{m}^2$  device is in an isothermal state with its ambient. Examining equations (1), (4), and (5), we find that the noise parameters vary no more strongly than linear or inverse linear with the device junction temperature. Furthermore, perturbations of approximately 6K will only perturb the value of  $V_T$  by  $\sim 2\%$ . Therefore, we can expect temperature to have little impact on the extracted noise parameters.

## V. LARGE HBT ARRAYS AND AMPLIFIERS

Due to the large size of power transistors,  $r_B$ ,  $r_E$ , and  $V_T$  are difficult to obtain with high accuracy. However, base and/or emitter ballasting can increase the effective  $r_E$  and  $r_B$  such that they are easy to determine with the methods described above. The remaining parameter,  $V_T$ , grows in complexity significantly. Due to the poor thermal conductivity of GaAs and the high power densities of power amplifier operation, the junction temperature will be significantly higher than the ambient temperature. Furthermore, each device within an amplifier experiences a slightly different thermal environment. Figs. 11 and 12 compare  $F_{MIN}$  and  $R_n$ , respectively, for the  $896\mu\text{m}^2$  device where the array temperature is equal to the ambient. Despite these difficulties, the extracted noise parameters correlate well to the measured data.

## VI. CONCLUSIONS

The noise parameter extraction method described in [1] has been shown to correlate reasonably well to InGaP/GaAs SHBTs for wireless communication power amplifiers. However, issues concerning extracted noise parameter behavior over bias and frequency have yet to be reconciled.

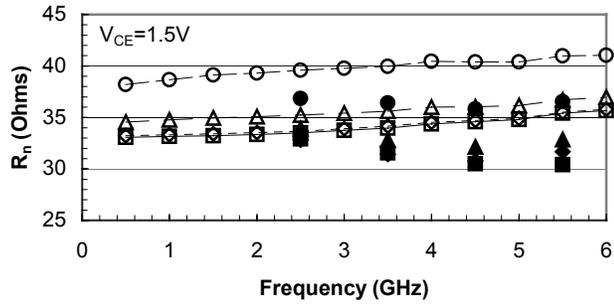


Fig. 7. Measured and extracted input referred noise of the  $56\mu\text{m}^2$  device.

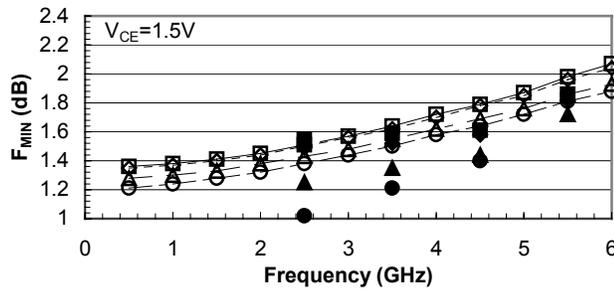


Fig. 8. Measured and extracted minimum noise figure of the  $56\mu\text{m}^2$  device. Line symbols are identical to those in Fig. 7.

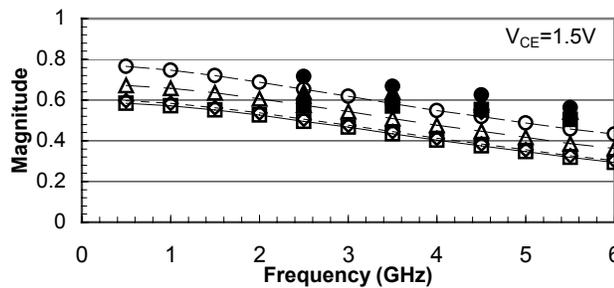


Fig. 9. Measured and extracted magnitude of  $\Gamma_{\text{SOP}}$  of the  $56\mu\text{m}^2$  device. Line symbols are identical to those in Fig. 7.

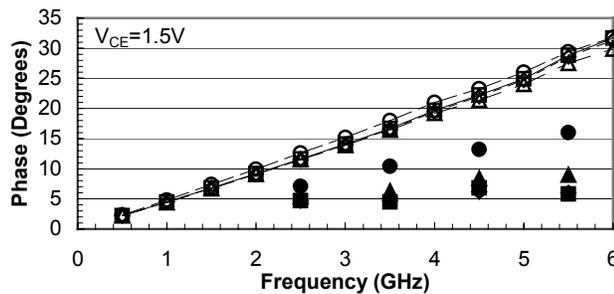


Fig. 10. Measured and extracted phase of  $\Gamma_{\text{SOP}}$  of the  $56\mu\text{m}^2$  device. Line symbols are identical to those in Fig. 7.

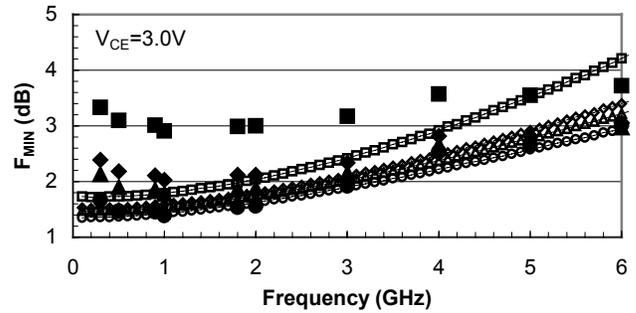


Fig. 11. Measured and extracted minimum noise figure of the  $896\mu\text{m}^2$  device. Array temperature is 25K and  $V_{\text{CE}} = 3.0\text{V}$ .

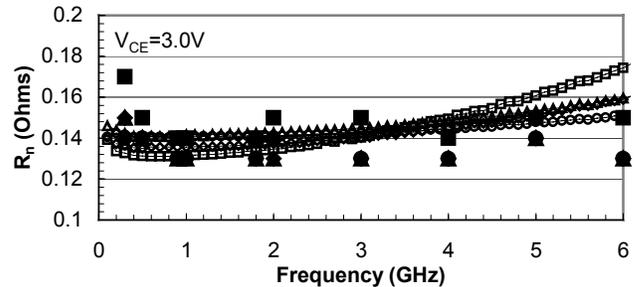


Fig. 12. Measured and extracted input referred noise of the  $896\mu\text{m}^2$  device. Array temperature is 25K and  $V_{\text{CE}} = 3.0\text{V}$ . Line symbols are identical to those in Fig. 11.

#### ACKNOWLEDGEMENTS

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#### ACRONYMS

- HBT: Hetero-junction Bipolar Transistor
- SHBT: Single Hetero-junction Bipolar Transistor
- BJT: Bipolar Junction Transistor